#### CARBON and OXYGEN

SHELL-NODAL STRUCTURE

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http://shpenkov.janmax.com/CarbonOxygen.pdf

#### Particular solutions of the wave equation in spherical polar coordinates

$$\Delta \hat{\Psi} - \frac{1}{c^2} \frac{\partial^2 \hat{\Psi}}{\partial t^2} = 0 \tag{1}$$

The wave equation (1) admits the particular solutions in the form

$$\hat{\Psi}(\mathbf{r},t) = \hat{\psi}(\mathbf{r})e^{\pm i\omega t} \quad (\omega = kc)$$
 (2)

where

$$\hat{\psi}(\mathbf{r}) = \hat{R}(kr)\Theta(\theta)\hat{\Phi}(\varphi)$$

is a particular solution of the corresponding Helmholtz equation

$$\Delta \hat{\psi} + k^2 \hat{\psi} = 0 \,; \tag{3}$$

The separation of variables leads to one time equation

$$\frac{d^2\hat{T}}{d\tau^2} = -\hat{T} \tag{4}$$

and three equations of the spherical space:

$$\rho^{2} \frac{d^{2} \hat{R}_{l}}{d \rho^{2}} + 2\rho \frac{d \hat{R}_{l}}{d \rho} + (\rho^{2} - l(l+1))\hat{R}_{l} = 0$$
(5)

$$\frac{d^2\Theta_{l,m}}{d\theta^2} + ctg\theta \frac{d\Theta_{l,m}}{d\theta} + \left(l(l+1) - \frac{m^2}{\sin^2\theta}\right)\Theta_{l,m} = 0$$
 (6)

$$\frac{d^2\hat{\Phi}_m}{d\varphi^2} + m^2\hat{\Phi}_m = 0 \tag{7}$$

where  $\rho = kr$  and  $\tau = \omega t$ .

The time component is usually presented in the form

$$\hat{T}(\omega t) = e^{i\omega t} \tag{8}$$

The **general form of the solutions** of the wave equation (1) for the spherical (longitudinal, central) component of  $\hat{\Psi}$ , in **spherical polar coordinates**, is

$$\hat{\Psi} = \hat{R}_l(kr)\Theta_{l,m}(\theta)\hat{\Phi}_m(\phi)\hat{T}(\omega t) \tag{9}$$

where  $\hat{\Psi} = \hat{R}_l(kr)\Theta_{l,m}(\theta)\hat{\Phi}_m(\phi)$  is the **spatial factor** of the wave function of physical space;  $l = 0, 1, 2, ...; m = 0, \pm 1, \pm 2, ..., \pm l$ .

The **radial component**  $\hat{R}_l(kr)$  of the spatial factor describes the **density of potential-kinetic probability of radial displacements**, the **polar component**  $\Theta_{l,m}(\theta)$  – the **polar displacements**, and  $\hat{\Phi}_m(\phi)$  – the **azimuth displacements**.

Under the above conditions, at integer values of the wave number m, an **elementary solution of the wave equation has the standard form**. If we present the number m in the form  $m = \frac{1}{2}2s$ , where  $s \in N$ , we arrive at

$$\hat{\Psi} = A_l \hat{R}_l(\rho) \Theta_{l,s}(\theta) e^{\pm is\phi} = A_l \sqrt{\pi/2\rho} H_{l+\frac{1}{2}}^{\pm}(\rho) \Theta_{l,s}(\theta) e^{\pm is\phi}$$
(10)

or

$$\hat{\Psi} = A_l \sqrt{\pi/2\rho} (J_{l+\frac{1}{2}}(\rho) \pm i Y_{l+\frac{1}{2}}(\rho)) \Theta_{l,s}(\theta) e^{\pm i s \phi}, \tag{11}$$

where  $A_l$  is the constant factor;  $\rho = kr$ ;

$$H_{l+\frac{1}{2}}^{\pm}(\rho)$$
,  $J_{l+\frac{1}{2}}(\rho)$  and  $Y_{l+\frac{1}{2}}(\rho)$  (or  $N_{l+\frac{1}{2}}(\rho)$ ) are the

Hankel, Bessel and Neumann functions, correspondingly.

Two terms in (11) are the **potential** and **kinetic spatial** constituents of  $\hat{\Psi}$  function; they have the following form

$$\hat{\Psi}_p = Ac_l(\rho)/\rho = A\sqrt{\pi/2\rho}J_{l+\frac{1}{2}}(\rho)\Theta_{l,m}(\theta)e^{\pm im\varphi}$$
(12)

$$\hat{\Psi}_k = \pm A s_l(\rho) / \rho = \pm A \sqrt{\pi / 2\rho} Y_{l+\frac{1}{2}}(\rho) \Theta_{l,m}(\theta) e^{\pm im\varphi}$$
(13)

The **half-integer solutions** of (3), at l = m = (1/2)s, have the form

$$\hat{\Psi} = A\hat{R}_s(\rho)\Theta_s(\theta)e^{\frac{\pm i\frac{3}{2}\phi}{2}} \tag{14}$$

where

$$\hat{R}_{s}(\rho) = \sqrt{\pi/2\rho} H_{\frac{s}{2} + \frac{1}{2}}^{\pm}(\rho)$$
 (15)

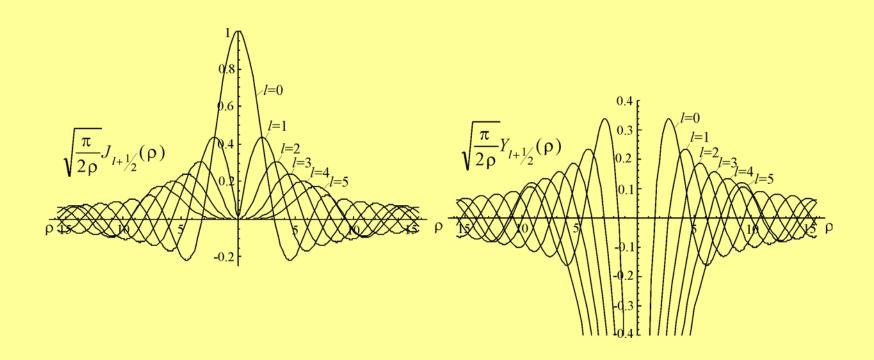
$$\Theta_s(\theta)e^{\pm i\frac{s}{2}\phi} = C_s \sin^{\frac{s}{2}}\theta(\cos\frac{s}{2}\phi \pm i\sin\frac{s}{2}\phi)$$
 (16)

The polar extremes of half-integer solutions lie in the equatorial plane.

## The Radial Solutions for the Wave Equation

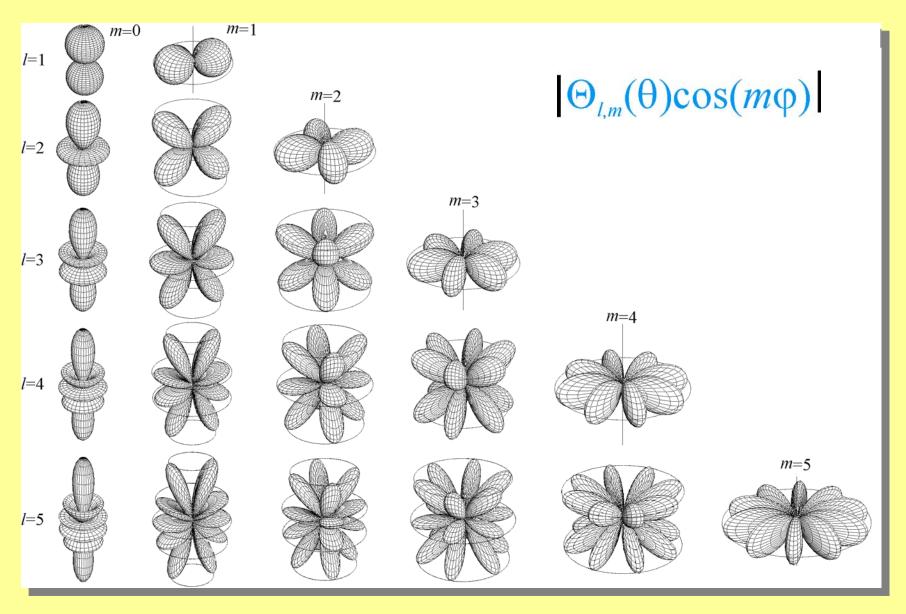
$$\begin{split} I & \hat{R}_{l}(\rho)/A = \hat{e}_{l}(\rho)/\rho = \sqrt{\pi/2\rho} (J_{l+\frac{1}{2}}(\rho) \pm iY_{l+\frac{1}{2}}(\rho)) \\ 0 & (\sin\rho \pm i (-\cos\rho))/\rho \\ 1 & ((\rho^{-1}\sin\rho - \cos\rho) \pm i (-\rho^{-1}\cos\rho - \sin\rho)) \rho^{-1} \\ 2 & [((3\rho^{-2} - 1)\sin\rho - 3\rho^{-1}\cos\rho)) \pm i ((1 - 3\rho^{-2})\cos\rho - 3\rho^{-1}\sin\rho))] \rho^{-1} \\ 3 & [((15\rho^{-3} - 6\rho^{-1})\sin\rho + (1 - 15\rho^{-2})\cos\rho) \pm i (-(15\rho^{-3} - 6\rho^{-1})\cos\rho + \\ & + (1 - 15\rho^{-2})\sin\rho)]\rho^{-1} \\ 4 & [((1 - 45\rho^{-2} + 105\rho^{-4})\sin\rho + (10\rho^{-1} - 105\rho^{-3})\cos\rho) \pm \\ & \pm i (-(1 - 45\rho^{-2} + 105\rho^{-4})\cos\rho + (10\rho^{-1} - 105\rho^{-3})\sin\rho)] \rho^{-1} \\ 5 & [((945\rho^{-5} - 420\rho^{-3} + 15\rho^{-1})\sin\rho - (945\rho^{-4} - 105\rho^{-2} + 1)\cos\rho) \pm \\ & \pm i (-(945\rho^{-5} - 420\rho^{-3} + 15\rho^{-1})\cos\rho - (945\rho^{-4} - 105\rho^{-2} + 1)\sin\rho)] \rho^{-1} \end{split}$$

#### Plots of the First Six Radial Spherical Functions

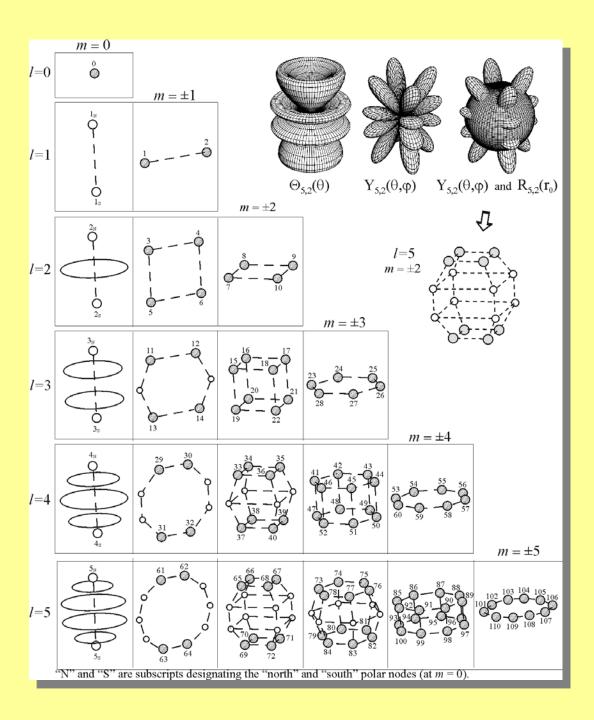


## Reduced Polar-Azimuthal Potential Functions

1	m	$\vec{Y}_{l,m}(oldsymbol{ heta},arphi) =  ilde{\mathscr{O}}_{l,m}(oldsymbol{ heta}) \operatorname{cos} m arphi$	l	m	$ ilde{Y}_{l,m}( heta,arphi)= ilde{ heta}_{l,m}( heta)\cos marphi$
0	0	1			
1	0	$\cos\theta$	5	0	$\cos\theta (\cos^4\theta - 10/9\cos^2\theta + 5/21)$
	±1	$\sin\theta\cos\varphi$		±1	$\sin\theta(\cos^4\theta - 2/3\cos^2\theta + 1/21)\cos\varphi$
2	0	$\cos^2\theta$ - 1/3		±2	$\sin^2\theta\cos\theta(\cos^2\theta - 1/3)\cos^2\varphi$
	±1	$\sin\theta\cos\theta\cos\varphi$		±3	$\sin^3\theta (\cos^2\theta - 1/9)\cos^3\varphi$
	±2	$\sin^2\theta \cos 2\varphi$		±4	$\sin^4\theta \cos\theta \cos 4\varphi$
3	0	$\cos\theta (\cos^2\theta - 3/5)$		±5	$\sin^5\theta \cos 5\varphi$
	±1	$\sin\theta (\cos^2\theta - 1/5)\cos\varphi$			
	±2	$\sin^2\theta \cos\theta \cos 2\varphi$	6	0	$\cos^6\theta - 15/11\cos^4\theta + 5/11\cos^2\theta - 5/231$
	±3	$\sin^3\theta \cos 3\varphi$		±1	$\sin\theta\cos\theta(\cos^4\theta - 10/11\cos^2\theta + 5/33)\cos\varphi$
4	0	$\cos^4\theta - 6/7\cos^2\theta + 3/35$		±2	$\sin^2\theta(\cos^4\theta - 6/11\cos^2\theta + 1/33)\cos^2\varphi$
	±1	$\sin\theta\cos\theta(\cos^2\theta - 3/7)\cos\varphi$		±3	$\sin^3\theta \cos\theta (\cos^2\theta - 3/11) \cos^3\theta$
	±2	$\sin^2\theta (\cos^2\theta - 1/7)\cos^2\varphi$		±4	$\sin^4\theta (\cos^2\theta - 1/11) \cos^4\theta$
	±3	$\sin^3\theta \cos\theta \cos 3\varphi$		±5	$\sin^5\theta \cos\theta \cos 5\varphi$
	±4	$\sin^4\theta \cos 4\varphi$		±6	$\sin^6\theta \cos 6\varphi$



Graphs of the polar-azimuthal functions

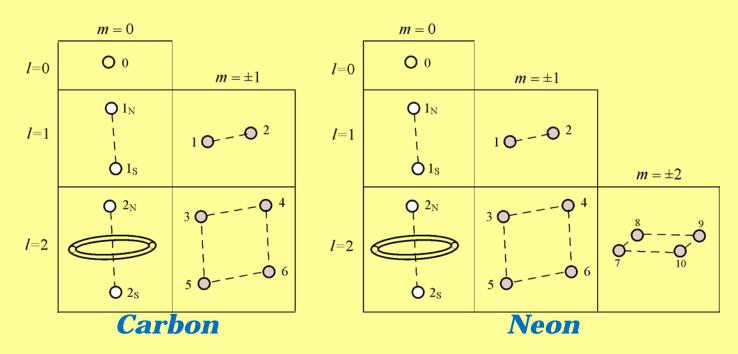


A spatial disposition of polar nodes and rings (m=0), and polar-azimuthal potential nodes (m≠0)

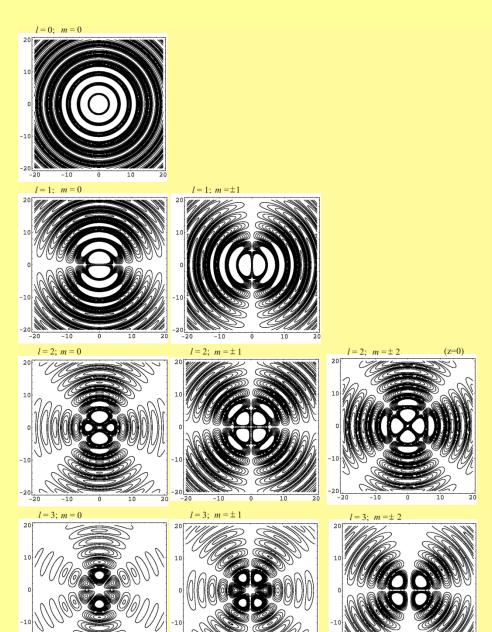
(soltutions of the wave equation)

$$\Delta \widehat{\Psi} - \frac{1}{c^2} \frac{\partial^2 \widehat{\Psi}}{\partial t^2} = 0$$

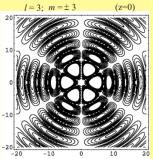
## A schematic drawing of the nodes and a toroidal vortex-ring in the carbon and neon atoms

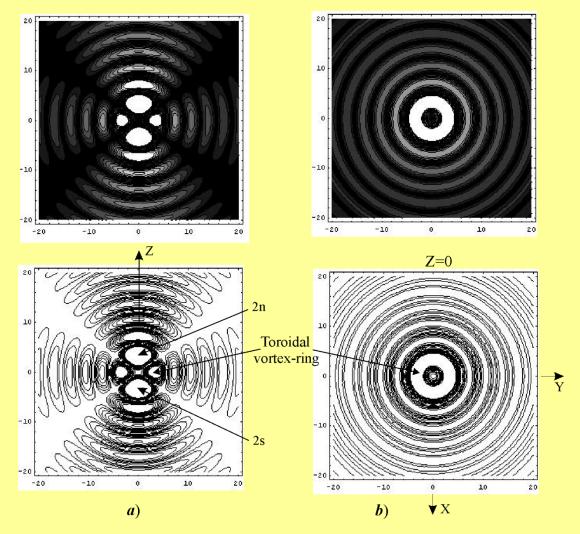


 $0, 1_N, 1_S, 2_N, 2_S$  are the ordinal number of the polar potential-kinetic nodes (located along the z-axis, m=0); 1, 2,..., 10 are the ordinal numbers of principal polar-azimuthal potential nodes. The nodes 1 and 2 belong to the internal spherical shell, l=1; the nodes 3-10 are located on the external spherical shell, l=2.



Contour plots of sections for the potential density of probability  $\Psi_p$  in a plane x=0 (and z=0 for l=2,  $m=\pm 2$ ; l=3,  $m=\pm 3$ )





A solution of the wave equation for a spherical shell of the atoms with the wave (quantum) numbers l=2, m=0: (a) for a section along the z-axis (in a plane perpendicular to the plane (x, y)), (b) for a section z=0 in a plane (x, y); 2n and 2s are, respectively, the north and south polar nodes of the shell

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#### PERIODIC TABLE

Numbers 1, 2, 3, ..., 110 are the ordinal numbers of the principal polar-azimuth nodes coinciding with



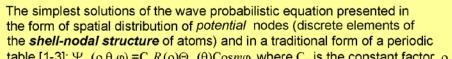
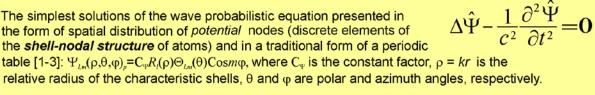
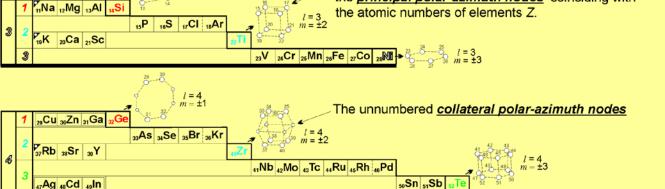


table [1-3]:  $\Psi_{I,m}(\rho,\theta,\phi)_m = C_w R_I(\rho)\Theta_{I,m}(\theta) Cosm\phi$ , where  $C_w$  is the constant factor,  $\rho = kr$  is the





¶ | ₁H

₃Li ⊿Be

112 113 114

120

115 116

117

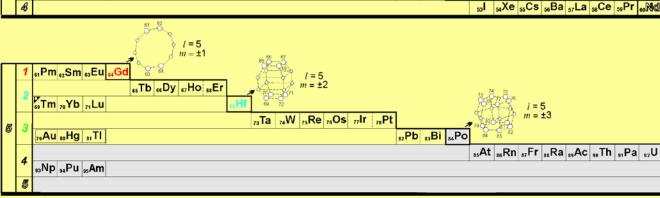
۶B

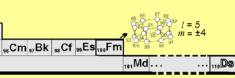
γN

Elements with the completely filled outer nucleonic shells

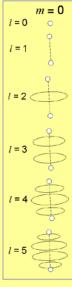
₂H®				
<sub>6</sub> С	10N®			
14Si	<sub>22</sub> Ti	28 <b>N</b> I		
32Ge	40Zr	<sub>52</sub> Te	eo Nd	
64 <b>Gd</b>	72 <b>Hf</b>	84Ро	100Fm	110DS

is the designation of unstable elements



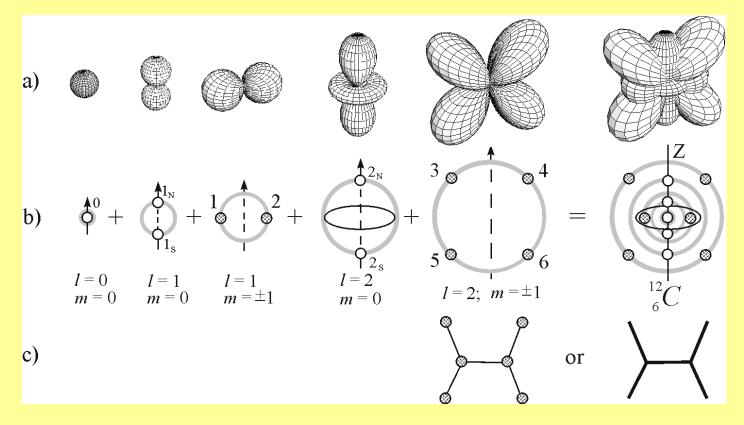


#### Polar nodes and rings

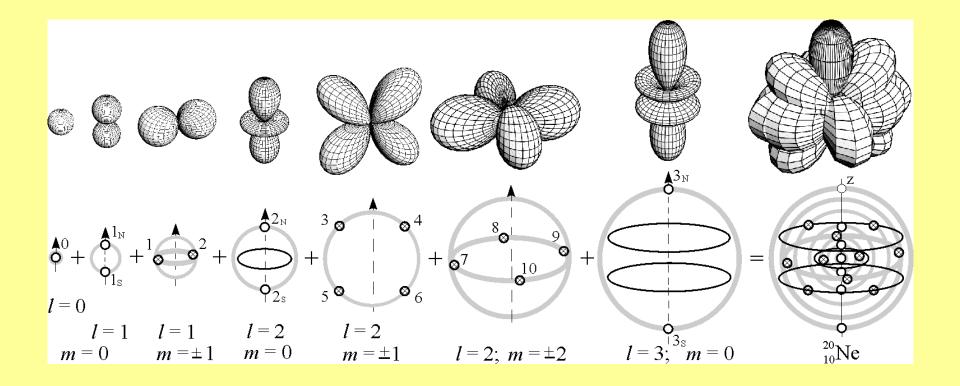


[1] Alternative Picture of the World, V. 1-3, (1996); [2] Foundations of Physics, (1998)

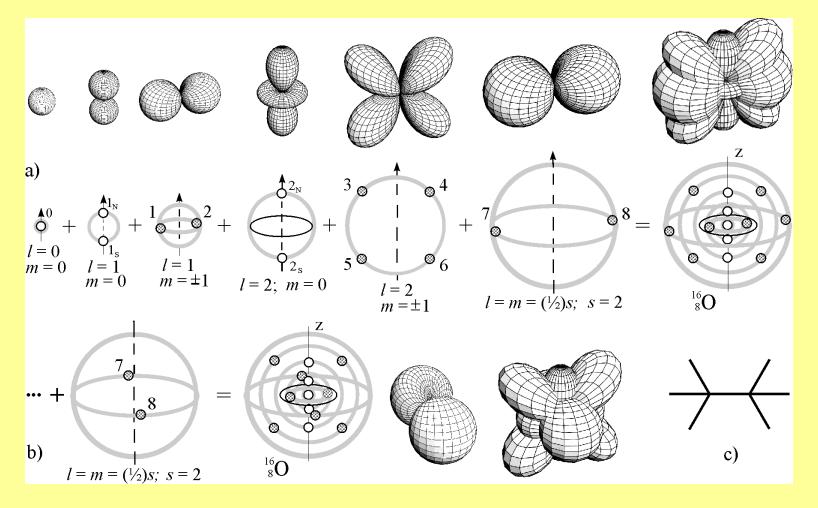
[3] Atomic Structure of Matter-Space, (2001); Geo. S., Bydgoszcz by L. Kreidik and G. Shpenkov.



- (a) Plots of potential-kinetic polar and potential polar-azimuthal functions;
- (b) polar and potential nodes on spherical shells;
- (c) symbolic designations of the carbon atom



- (a) Plots of potential-kinetic polar and potential polar-azimuthal functions;
- (b) polar and potential nodes on spherical shells;
- (c) symbolic designations of the neon atom



- (a) Plots of potential-kinetic polar and potential polar-azimuthal functions;
- (b) polar and potential nodes on spherical shells;
- (c) symbolic designations of the oxygen atom

#### The Relative Atomic Mass

$$A = \sum_{k} Z_{pk} \eta_{pk} + \sum_{i} (Z_{gi} \eta_{gi} + Z_{vi} \eta_{vi})$$

**k**, *i* are the numbers of polar (m = 0) and polar-azimuthal  $(m \neq 0)$  shells, respectively;

 $\mathbb{Z}_{p,k}$  is the number of polar nodes of k-th polar shell;

 $\mathbf{Z}_{gi}$  and  $\mathbf{Z}_{vi}$  are the number of principal and collateral polar-azimuth nodes, respectively, of i-th polar-azimuthal shell;

 $\eta_{pk}$ ,  $\eta_{gi}$ , and  $\eta_{vi} = 0$ , 1, or 2 is the multiplicity of filling of the nodes by H-atoms.

#### The Matrices of the Nodes of Carbon and Oxygen Atoms

(potential-kinetic polar and potential polar-azimuthal)

$$|C_{l,m}| = \begin{vmatrix} 1 & 0 & 0 \\ 2 & 2 & 0 \\ 2 & 4 & 0 \end{vmatrix}$$
  $|O_{l,m}| = \begin{vmatrix} 1 & 0 & 0 \\ 2 & 2 & 0 \\ 2 & 4 & 2 \end{vmatrix}$ 

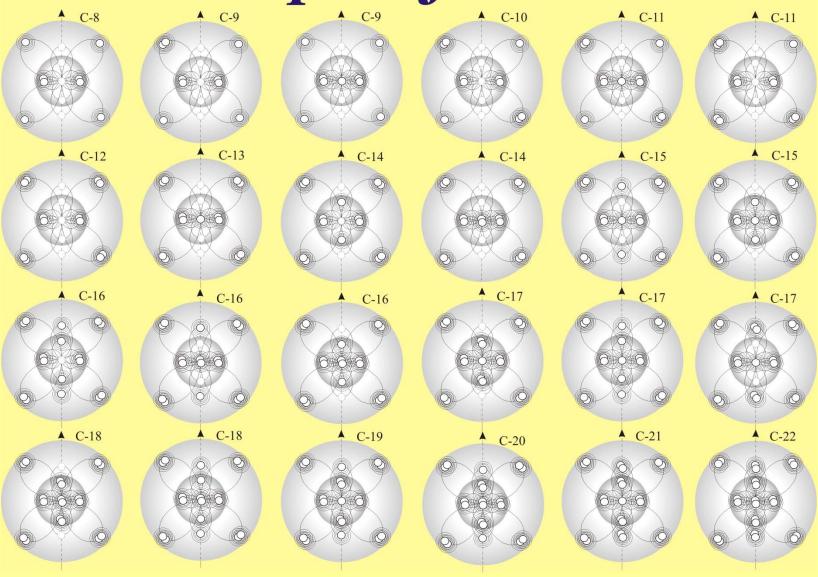
$$\left| \mathbf{O}_{l,m} \right| = \begin{vmatrix} 1 & 0 & 0 \\ 2 & 2 & 0 \\ 2 & 4 & 2 \end{vmatrix}$$

The matrices of filing of the nodes by H-atoms in the stable, lightest, and heaviest isotopes of the carbon and oxygen atoms

$$|\begin{smallmatrix}12\\6\\C | = \begin{vmatrix}0 & 0 & 0\\0 & 4 & 0\\0 & 8 & 0\end{vmatrix} \qquad |\begin{smallmatrix}8\\6\\C | = \begin{vmatrix}0 & 0 & 0\\0 & 4 & 0\\0 & 4 & 0\end{vmatrix} \qquad |\begin{smallmatrix}22\\6\\C | = \begin{vmatrix}2 & 0 & 0\\4 & 4 & 0\\4 & 8 & 0\end{vmatrix}$$

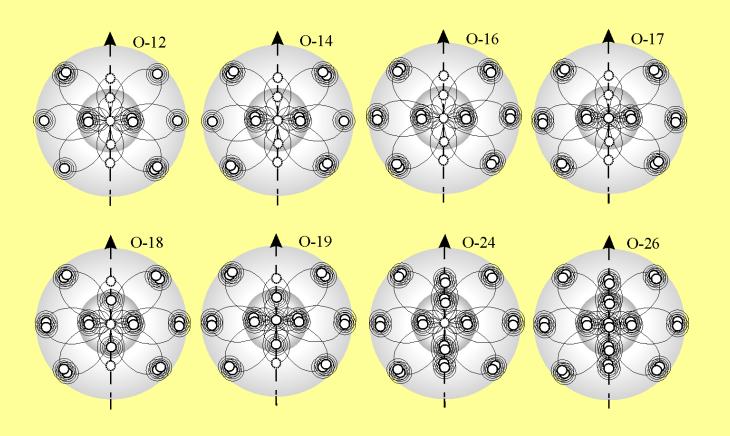
$$\begin{vmatrix} 1_{8}^{6}O \end{vmatrix} = \begin{vmatrix} 0 & 0 & 0 \\ 0 & 4 & 0 \\ 0 & 8 & 4 \end{vmatrix} \qquad \begin{vmatrix} 1_{2}^{12}O \end{vmatrix} = \begin{vmatrix} 0 & 0 & 0 \\ 0 & 4 & 0 \\ 0 & 6 & 2 \end{vmatrix} \qquad \begin{vmatrix} 1_{2}^{12}O \end{vmatrix} = \begin{vmatrix} 0 & 0 & 0 \\ 0 & 4 & 0 \\ 0 & 4 & 4 \end{vmatrix} \qquad \begin{vmatrix} 2_{6}^{6}C \end{vmatrix} = \begin{vmatrix} 2 & 0 & 0 \\ 4 & 4 & 0 \\ 4 & 8 & 4 \end{vmatrix}$$

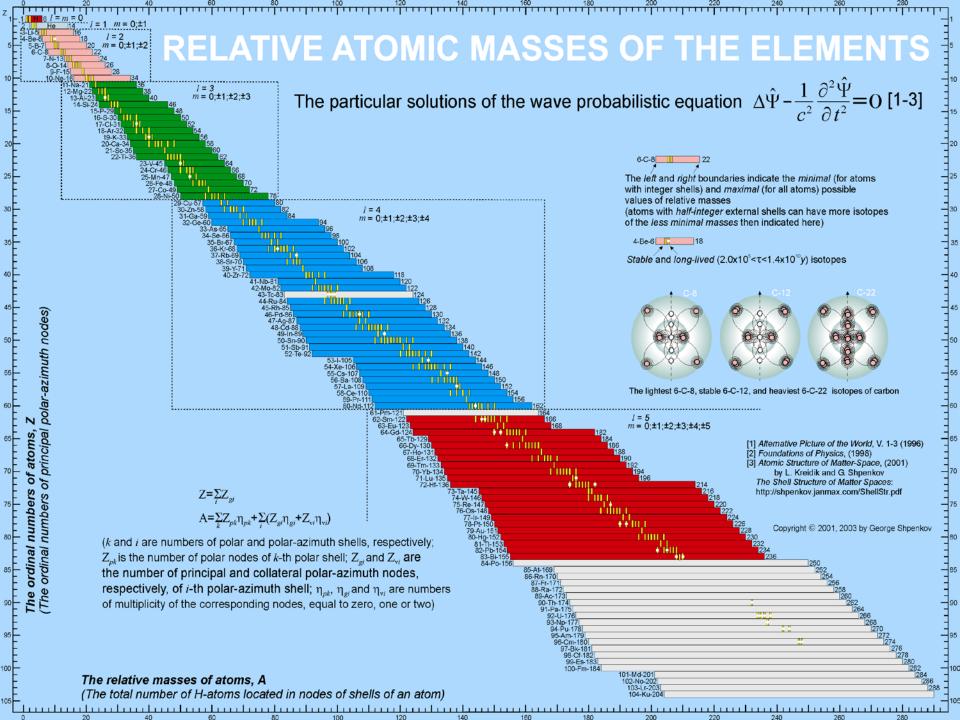
#### Isotopes of Carbon



### The shell-nodal structure of some isotopes of oxygen:

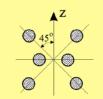
3 stable (160, 170 and 180) and 5 short-lived unstable (including lightest 120 and heaviest 260)





#### The Carbon Atom Structure





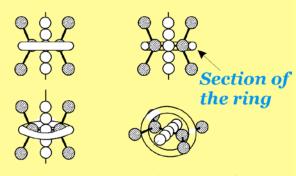


Direct image of the atom

Position of the Z axis

Main internodal bonds

( is an image of the potential node filled with 2 nucleons)



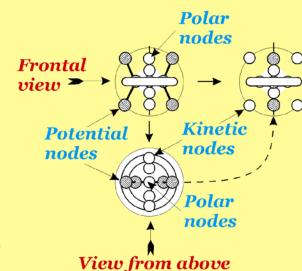
Position of polar nodes and a toroidal ring



Position of polar and kinetic nodes and a toroidal ring



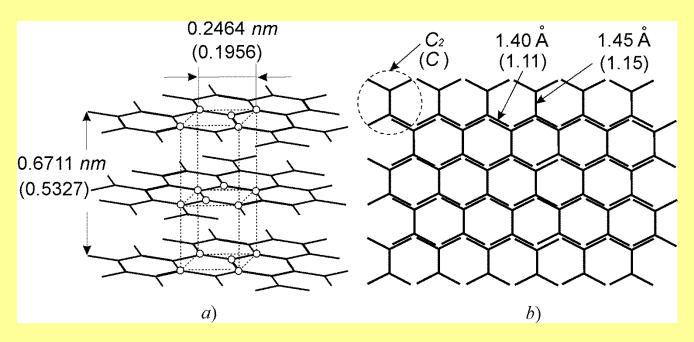
Conditional designation of the atom



View on the left side

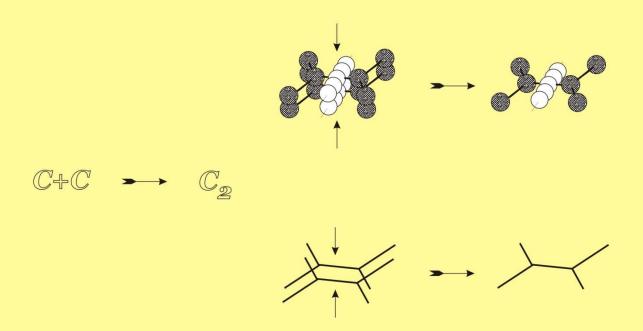
Mutual position of all constituents of the atom in three projections with indication of main bonds and external spherical shell

## An elementary cell of graphite



Lattice constants of graphite indicated in brackets correspond to Imaginary crystal lattice parameters if one account that the lattice is formed from single carbon atoms.

#### Formation of the C2 Molecule



Overlapping, "confluence", of all approaching nodes (and toroidal rings not shown here) of two carbon atoms in the unit whole.

(An image of C2 does not differ from the image of a single C atom)

Precise calculations of atomic positions and the length of interatomic bonds are based on an iterative method. The latter includes a comparison and fitting of measured intensities of a reflected beam with calculated ones and with due account of Rutherford-Bohr's nuclear model of atoms, so as long as will not be achieved an adequate correspondence of two sets of the values.

Obviously, if only a structural analysis would be based on a shell-nodal (i.e., multi-center or molecule-like) atomic model, the gauging would be different; depending on what is accepted in the capacity of an elementary "building block" of crystal lattices — a molecule-like atom or a carbon dimer, C or C2 in our case.

Assuming that the lattice constants of crystals accepted in physics are precise and congruent to reality, we must accept that an elementary "building block" of carbon crystals is the C2 diatomic molecule.

#### Carbon Dimer (C2)

is

in fact the major observable product of C60 fragmentation.

Being a very effective growth species, it can rapidly incorporate into the diamond lattice leading to high-film growth rates\*.

\* [D. M. Gruen, at al, *Turning Soot Into Diamonds With Microwaves*, Proceedings of the 29<sup>th</sup> Microwave Power Symposium, Chicago, Illinois, July 25-27, 1994].

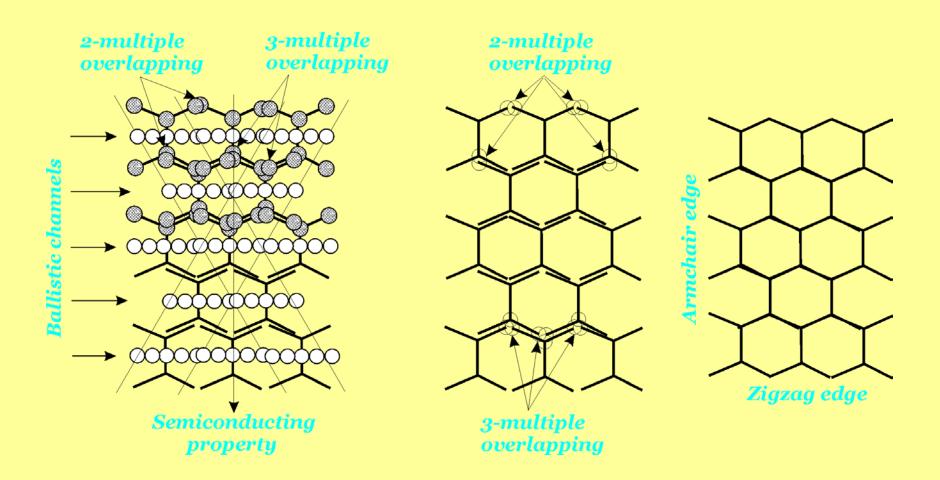
And as follows from the work referred below,

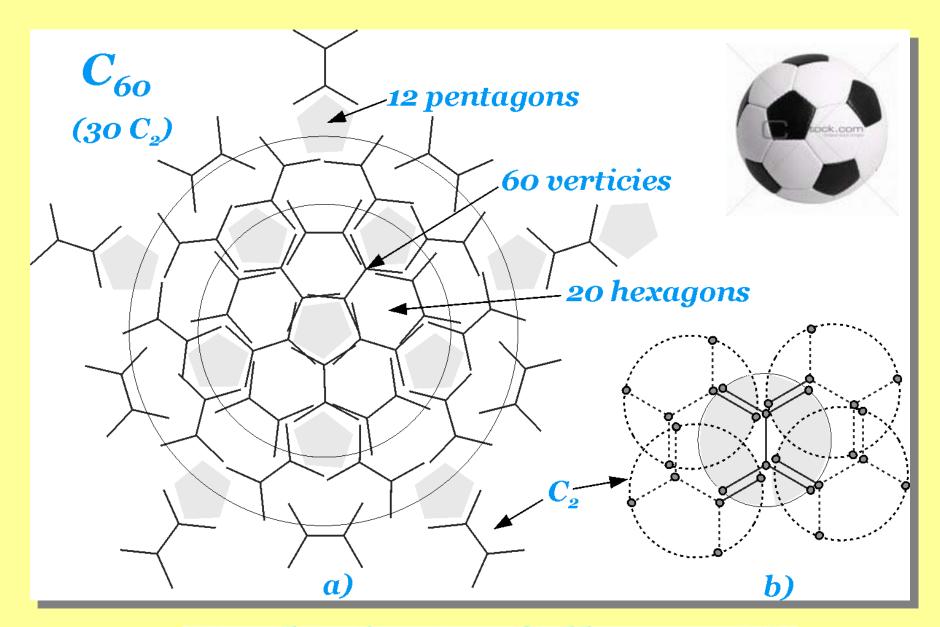
"the C2 radical was considered to be responsible for the formation of graphite"\*\*

\*\* [H. C. Shik, et al., *Diamond and Related Materials*, 2, 531 (1993)],

A schematic view of self-binding (assembling) of two-dimensional carbon compounds

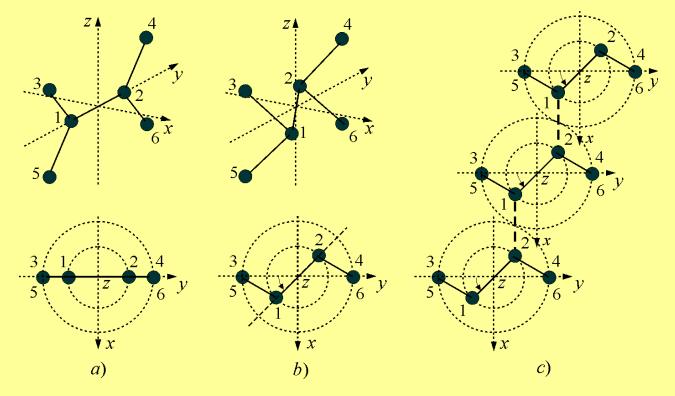
#### A part of a graphene sheet



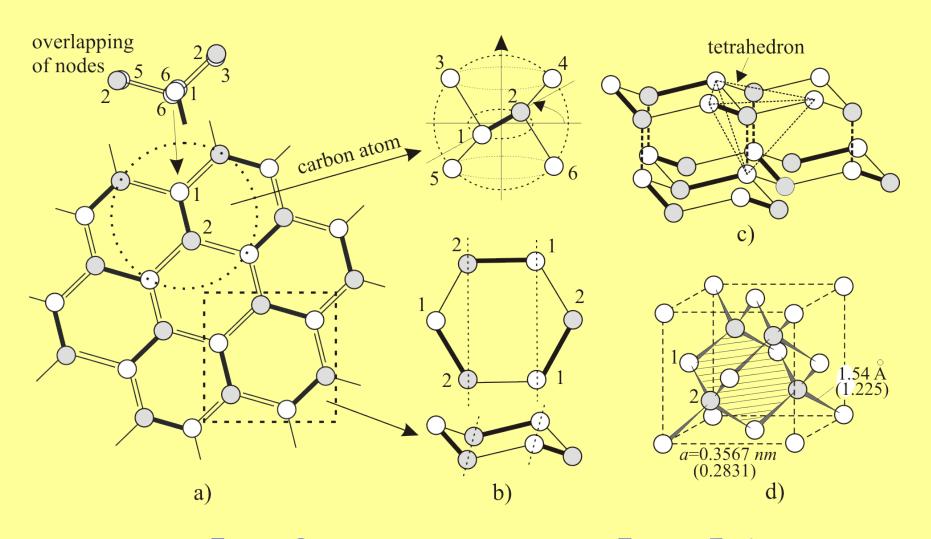


Buckminsterfullerene C<sub>60</sub>

#### The Formation of Bonds in Diamond

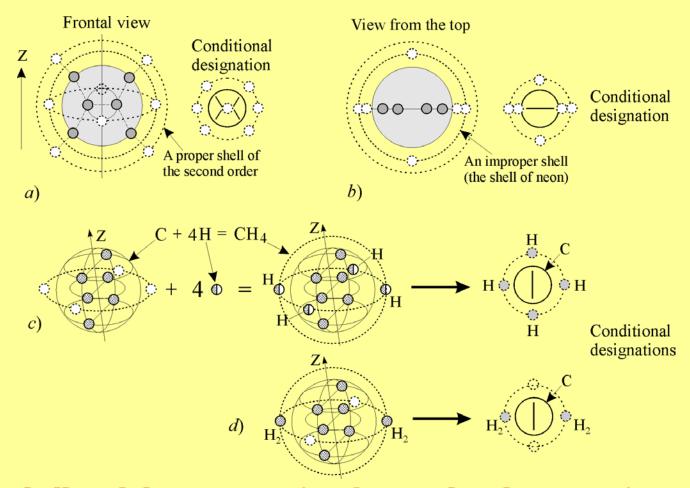


- (a) A plane structure of the carbon atom (or molecule  $C_2$ );
- (b) a displaced position of its internal shell with nodes 1 and 2 around the z-axis by the phase angle  $\alpha = \pi/4$ ;
- (c) the bindings (dashed lines) between displaced internal nodes 1 and 2 of different carbon dimmers, resulted in a face-centered cube structure of diamond



The face centered cubic diamond lattice structure

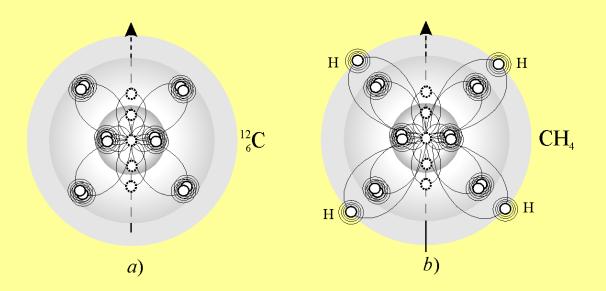
### Two Possible Ways (c, d) of the Formation of the methane molecule $CH_4$



(a, b) The shell-nodal structure of carbon with indication of two nearest, proper and improper, external spherical shells with their potential polar-azimuthal nodes designated by dotted lines.

### One more possible way of the formation of CH<sub>4</sub>

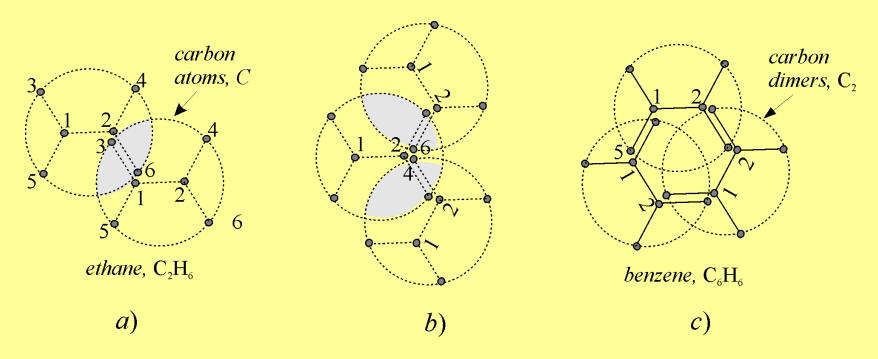
(A case of the participation of the second order proper radial shell of  $^{12}_{6}$ C in the formation of molecular bonds, resulted in a plane structure of the molecule)



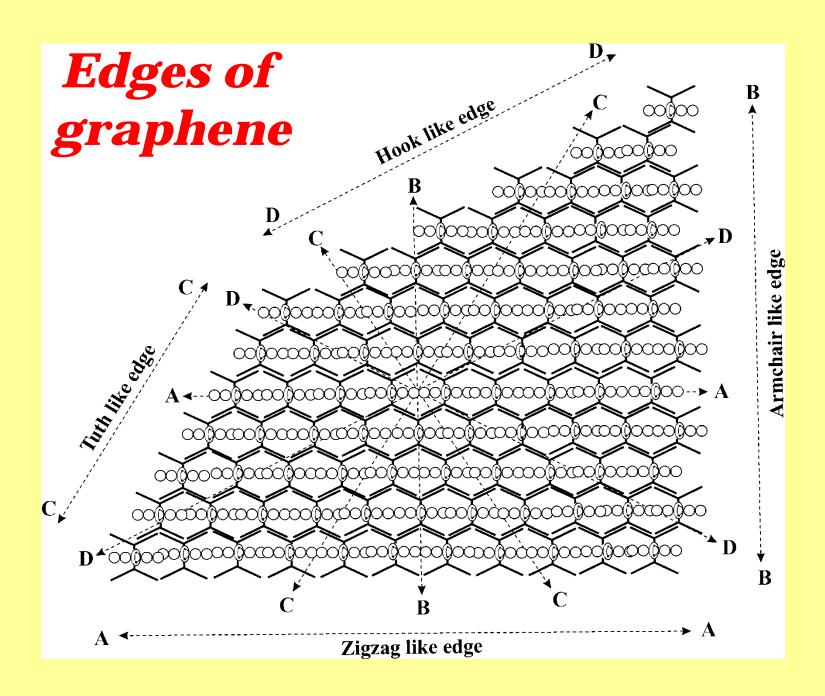
(a)An internal structure of the carbon atom  $^{12}_{6}$ C; (b) all chemically adsorbed individual H-atoms are in one plane with the completely filled by coupled H-atoms proper potential nodes of carbon

#### The Structure of Bindings in Typical Hydrocarbon Compounds

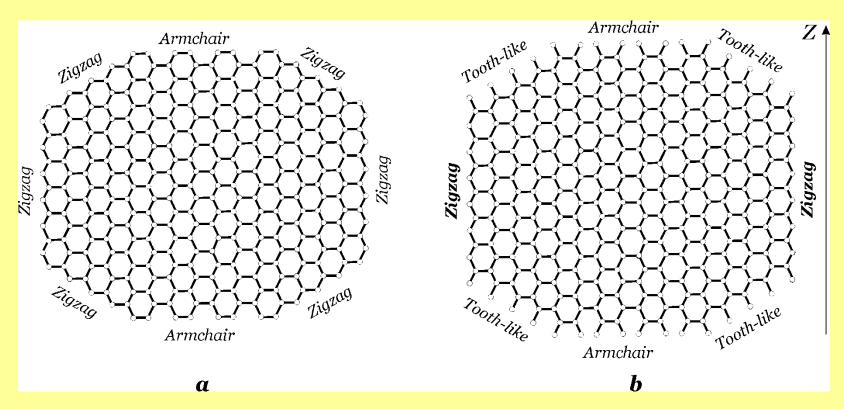
# A schematic view showing how C – C bonds are formed in hydrocarbon compounds



The character of overlapping (two- and three-multiple) of polar-azimuthal nodes for the case of single carbon atoms (a) and their dimmers (b, c)



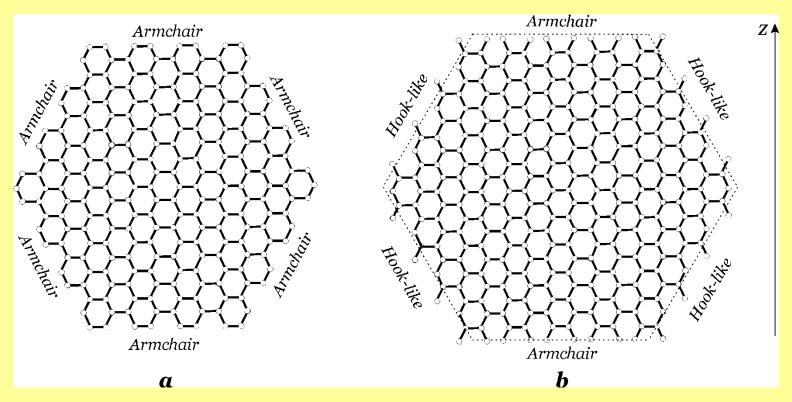
### Two images of graphene edges



Incorrect (overall used)

**Correct** 

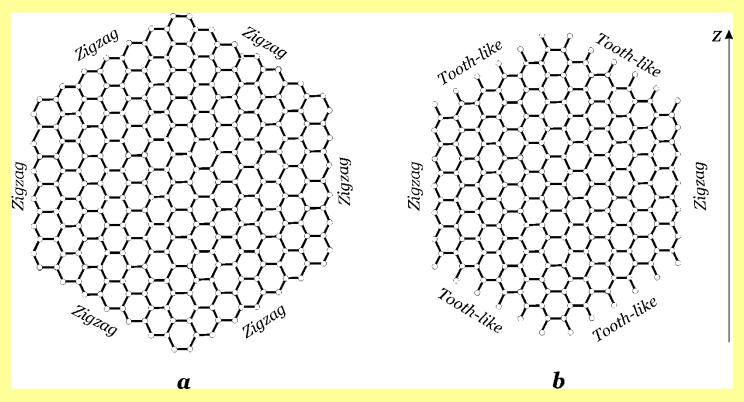
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**Correct** 

### Two images of graphene edges

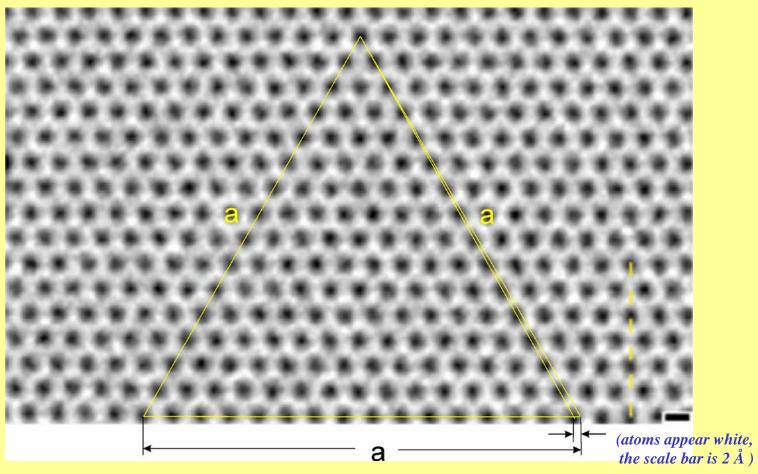


Incorrect (overall used)

**Correct** 

### Direct Image of a Single-Layer Graphene Membrane\*

(with our findings)



\*[J.C. Meyer, C. Kisielowski, R. Erni, M.D. Rossell, M.F. Crommie, and A. Zettl. *Direct imaging of lattice atoms and topological defects in graphene membranes*. Nano Lett. 8 (11), 3582-3586 (2008)]

## Mechanism of the formation of typical metastable pentagon-heptagon (5-7) defects inherent in graphene

(two pairs of five- and seven-membered rings of carbon nodes)

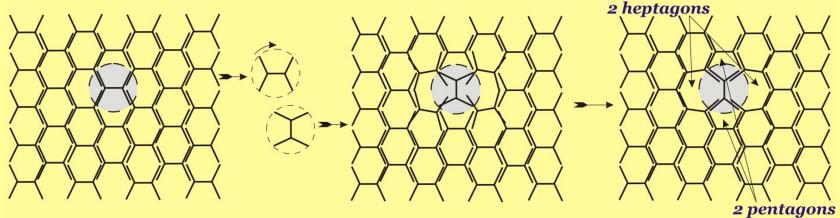
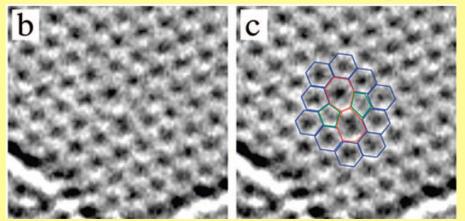


Figure 3\*. ...
(b) Stone-Walles (SW) defect
(c) same image with atomic
configuration superimposed



\*[J. C. Meyer at al.,Direct Imaging of Lattice Atoms and Topological Defects in Graphene Membranes, Nano Lett, 2008, 8 (11), 3582-3586]

# Formation of 4 pairs of five- and seven-membered rings of carbon nodes

"The study of defects, vacancies, and edges in graphene, as well as absorbates, is important for basic understanding of this novel material as well as for potential electronic, mechanical, and thermal applications"\*

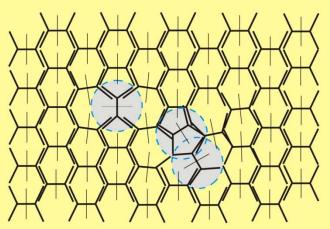
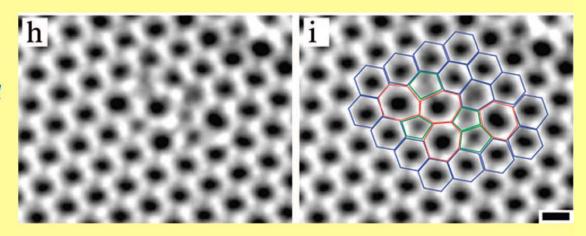


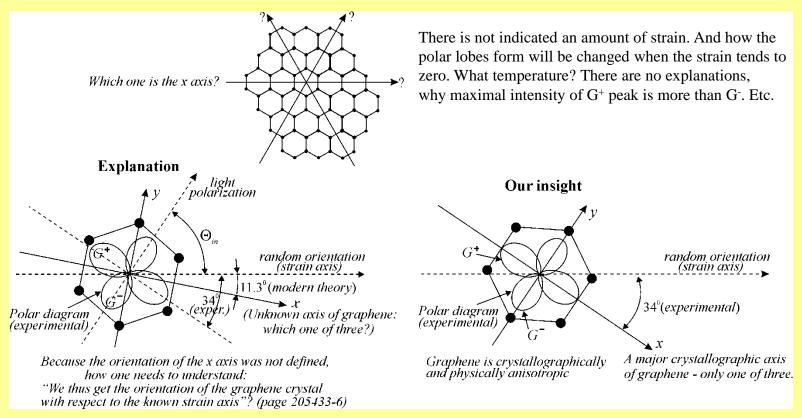
Figure 3\*....
(h and i) Defect image and configuration consisting of four pentagons (green) and heptagons (red)



\*[J. C. Meyer at al.,Direct Imaging of Lattice Atoms and Topological Defects in Graphene Membranes, Nano Lett, 2008, 8 (11), 3582-3586]

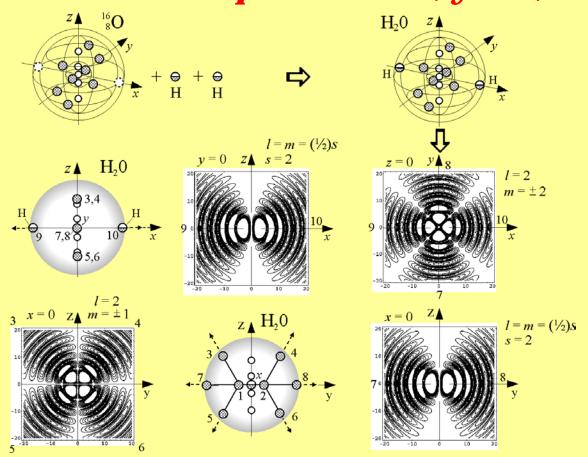
#### Our comments to the article

[Uniaxial strain in graphene by Raman spectroscopy: G peak splitting, Grüneisen parameters, and sample orientation, Phys. Rev. B 79, 205433 (8 pages), 2009 by T. M. G. Mohiuddin at al.]



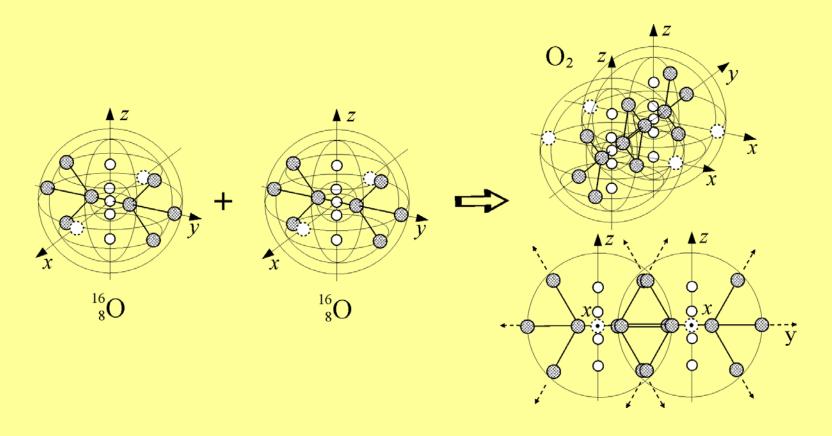
Mutually perpendicular axes of polar lobes are just characteristic crystallographic axes of graphene monolayer! The angles [Ref, Fig 6] between the strain axis and the axes of the lobes are equal to 34° and 56°, they are accidental in value, depending on an accidentally oriented graphene monolayer on a substrate in the experiment. A small difference in a maximal intensity of G<sup>+</sup> and G<sup>-</sup> peaks is related with the anisotropy of electrical conductivity. Thus, actually, authors of the paper, unknowing about this (not understanding it), have defined actually the orientation of characteristic crystallographic axes on a tested graphene monolayer, thus confirming that graphene is anisotropic.

A conditional image of the formation of the  $H_2O$  molecule, and the density of probability  $\widehat{\Psi}$  (contour plots) of the localization of matter in an external shell for the planes x = 0, y = 0, and z = 0

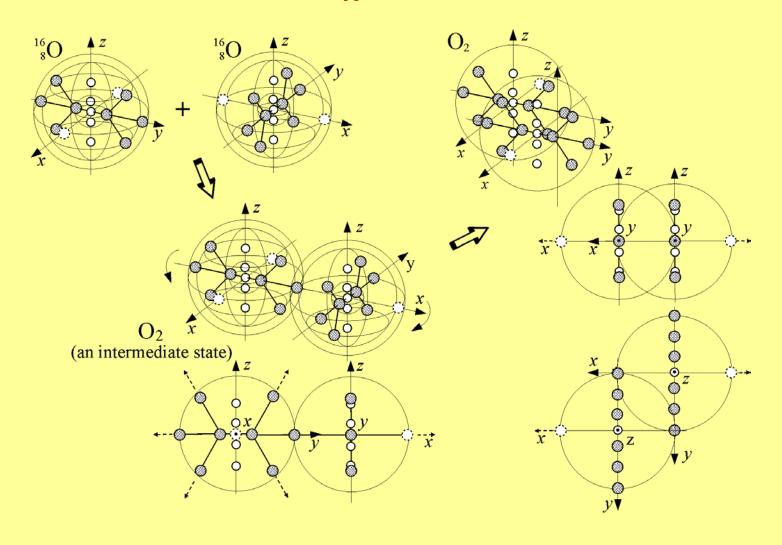


The dashed smaller arrows in the pictures indicate the main directions of external internodal bindings inherent in the water molecule

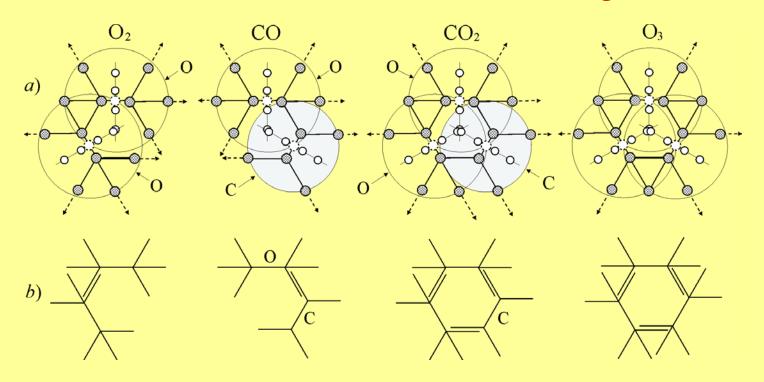
## A Possible Way of the Formation of the oxygen molecule O<sub>2</sub>



## One More Possible Way of the O<sub>2</sub> Formation

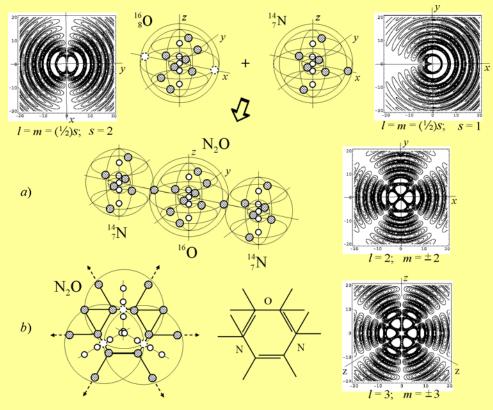


One more possible way of the formation of oxygen  $O_2$ , and the possible nodal structure of carbon oxide CO, carbon dioxide  $CO_2$ , and the ozone molecule  $O_3$  (a)



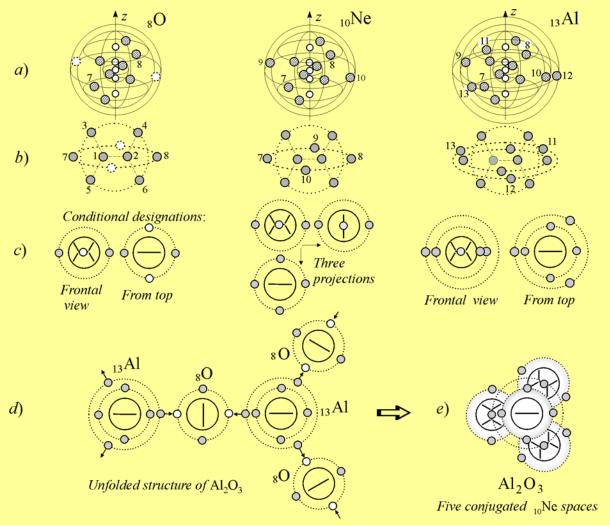
(b) symbolic designations of the compounds distinguished by the two-multiple overlapping of proper nodes of constituent atoms

## Two possible ways of the formation of hemioxide $N_2O$



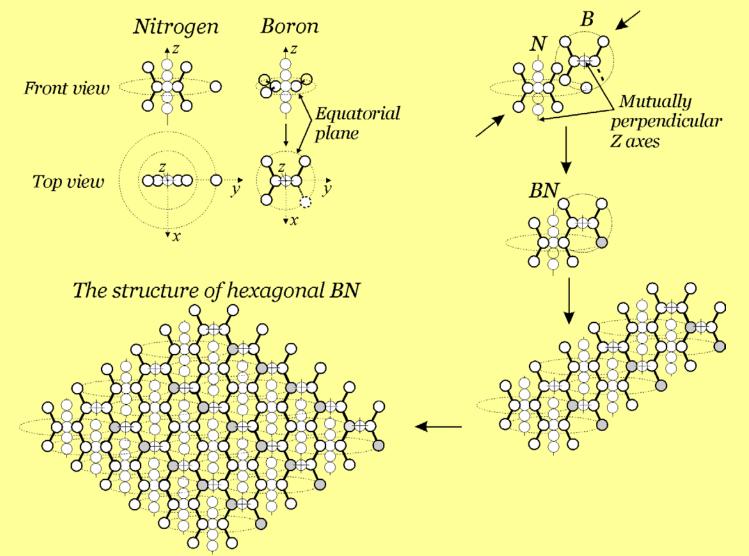
(a) an intermediate (unfolded) image of one of the ways, (b) another of the possible nodal bindings in the hypothetical  $N_2O$  structure. The equatorial densities of probability  $\widehat{\Psi}$  (contour plots) are drawn for external shells of separate atoms,  ${}^{16}_{8}O$  and  ${}^{14}_{7}N$  (the upper row, left and right); for the shell at  $l=2,m=\pm 2$  (the section for z=0); and for the external shell of the resulting formation  $(l=3,m=\pm 3)$ 

### The Shell-Nodal Structure of the Aluminum Oxide Al2O3



(a, b, c) the nodal structure of the atoms 0, Ne, and Al and their conditional designations for different projections; the unfolded (d) and closed (e) conditional images of the resulting  $Al_2O_3$  structure

### Formation of One-Atom-Thick Layer of Hexagonal Boron Nitride



#### CONCLUSION

We are on a threshold of uncovering the "genetic code" of structural variety in nature

http://shpenkov.janmax.com/CarbonOxygen.pdf